# Data Analysis Proposition 

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## Data Flows

## FR Metrics MOSes $y_{i, j}$

Indicators $x_{i, j}$

## Data Flows



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## Normalization

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- For HDTV it was set of subjective MOSes, for JEG-Hybrid it cannot be assumed
- Mean MOS of all metrics works the best probably


## Example



Input data


Normalized metrics

## Example with Errors



Input data


Normalized metrics

## Example Non Linear



Input data


Normalized metrics

## Example Non Linear with Errors



Input data


Normalized metrics

## Data Flows



## Single MOS or Multiple MOSes

- More points more information
- An alternative solution is regression including errors
- Is an error for 3-4 points really meaning full?
- If all points are used a perfect metric has $R^{2}$ different from 1 since the metrics inaccuracy makes the target function irrelevant


## Data Flows



## Removing not Relevant Points

- $\mid$ MOS $_{i, 1}-\left(a\right.$ MOS $\left._{i, 2}+b\right) \mid>\epsilon$ is changed to $\left|\hat{y}_{i, 1}-\hat{y}_{i, 2}\right|>\epsilon$.
- For many metrics $P V S_{j}$ is removed if $\max _{j}\left|\hat{y}_{i, j}-\hat{y}_{i, j}\right|>\epsilon$
- What should be $\epsilon$ value?
- Typical subjective experiment error? Which is?


## Data Flows



## PVS Grouping

- An indicator can work just for some PVSes (e.g. frame rate change only)
- Single PVS can be a member of many different groups
- Each analysis is performed on each group including all data
- Group of PVSes is a set of $i$ indexes $I_{k}$


## Analysis

Let us consider metric number 1

- Estimate $a$ and $b$ of a linear fit $\hat{y}_{i, j}=a x_{i, 1}+b$ for $i \in I_{k}$ and all $j$ and $k$
- Calculate $R^{2}$ for the obtained fit
- $x_{\cdot, 1}$ normalization by $\frac{x_{i, 1}-\bar{x}_{1}}{\sigma_{x_{i, 1}}}$ where $\sigma_{x_{i, 1}}$ is the standard deviation
- Estimate a cubic fit for $\hat{y}_{i, j}=\sum_{l=0}^{3} a_{l} x_{i, 1}^{l}$ for $i \in I_{k}$ and all $j$ and $k$
- Chucking p-values of $a_{l}$ - is the metric non linear?
- Calculate $R^{2}$ for the obtained fit


## Data Flows



## Analysis

- $x_{\cdot, 1}$ normalization by $\frac{x_{i, 1}-\bar{x}_{1}}{\sigma_{x_{i, 1}}}$ where $\sigma_{x_{i, 1}}$ is standard deviation
- Estimate a linear fit $\hat{y}_{i, j}=\sum_{l} a_{l} x_{i, b_{l}}+b$ for $i \in I_{k}$ and all $j, k$ and all possible combinations of $b_{l}$ values - if possible $\hat{y}_{i, j}=a_{1} x_{i, 1}+a_{2} x_{i, 2}+b ; \hat{y}_{i, j}=a_{1} x_{i, 1}+a_{2} x_{i, 3}+b ;$ $\hat{y}_{i, j}=a_{1} x_{i, 2}+a_{2} x_{i, 3}+b ; \hat{y}_{i, j}=a_{1} x_{i, 1}+a_{2} x_{i, 2}+a_{3} x_{i, 3}+b$
- First step is p-values analysis: is particular indicator statistically important?
- Removing not statistically important indicators and than adjust $R^{2}$ computation


## Analysis

- Metrics "cooperation" $\hat{y}_{i, j}=a_{0}+a_{1} x_{i, 1}+a_{2} x_{i, 2}+a_{3} x_{i, 1} x_{i, 2}$ for $i \in I_{k}$ and all $j$ and $k$
- First step is p-values analysis: is particular indicator statistically important? Looking especially on the metrics products coefficients
- Removing not statistically important indicators and than adjust $R^{2}$ computation

